



Thank you for joining us – the  
webinar will start shortly

# Longevity 101: *baseline*

February 11<sup>th</sup>, 2021

11am ET / 4pm GMT



@ClubVita



[linkedin.com/company/club-vita](https://www.linkedin.com/company/club-vita)

# Your panel



Erik Pickett PhD FIA CERA  
**Webinar chair**

Chief Content Officer,  
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Conor O'Reilly FFA  
**Panelist**

Head of Analytics,  
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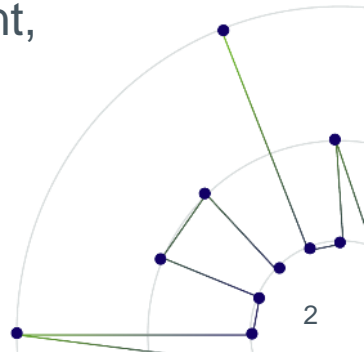
Shantel Aris ASA  
**Panelist**

Longevity Risk  
Modeler, Club Vita  
Canada



Steven Baxter FIA  
**Panelist**

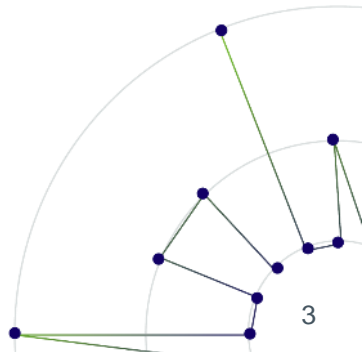
Head of Innovation  
and Development,  
Club Vita



# Agenda

1. Introduction
2. Standard tables
3. Factor based models
4. Experience analysis & credibility theory

Today we'll use the language of pension plans,  
- techniques apply to any group of lives



# 1 Introduction

# Jargon buster

**Longevity**



How long you are expected to live

**Survival rates  $p_x$**  - the probability a person aged  $x$  will survive the next year

**Longevity risk** - the risk of people living longer than expected

**Mortality**

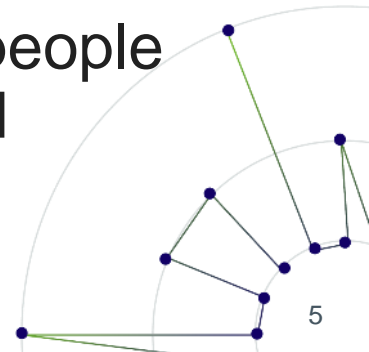


When you are expected to die

**Mortality rates  $q_x$**  - the probability a person aged  $x$  will die within the next year

**Mortality risk** - the risk of people dying sooner than expected

$$p_x = (1 - q_x)$$



## Life Expectancy

The expectation of the number of years a person will live.

Expressed as either

- “years left” (20 years Life Expectancy for a 65 year old); or
- “total years” (Total Life Expectancy of 85 for a 65 year old)

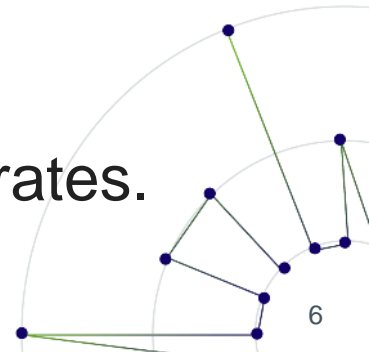


## Period Life Expectancy

Life expectancy based on mortality rates for one particular period – no allowance for any future changes in mortality rates

## Cohort Life Expectancy

Life expectancy of a person born in a certain year (cohort) allowing for expected future changes (usually improvements/reductions) in mortality rates.





# Two steps to calculate life expectancy



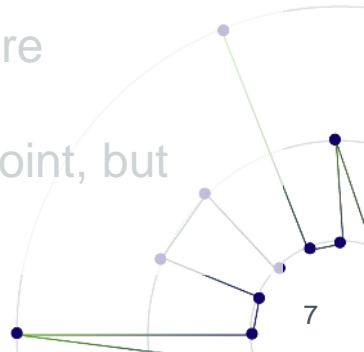
## Baseline

- Snapshot of current state of longevity
- Objective measure
- Based on past experience



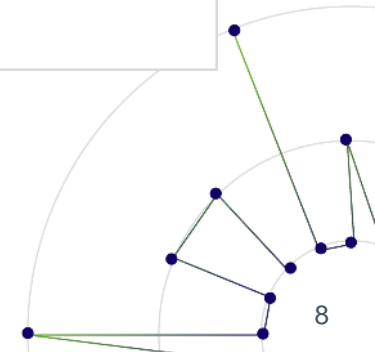
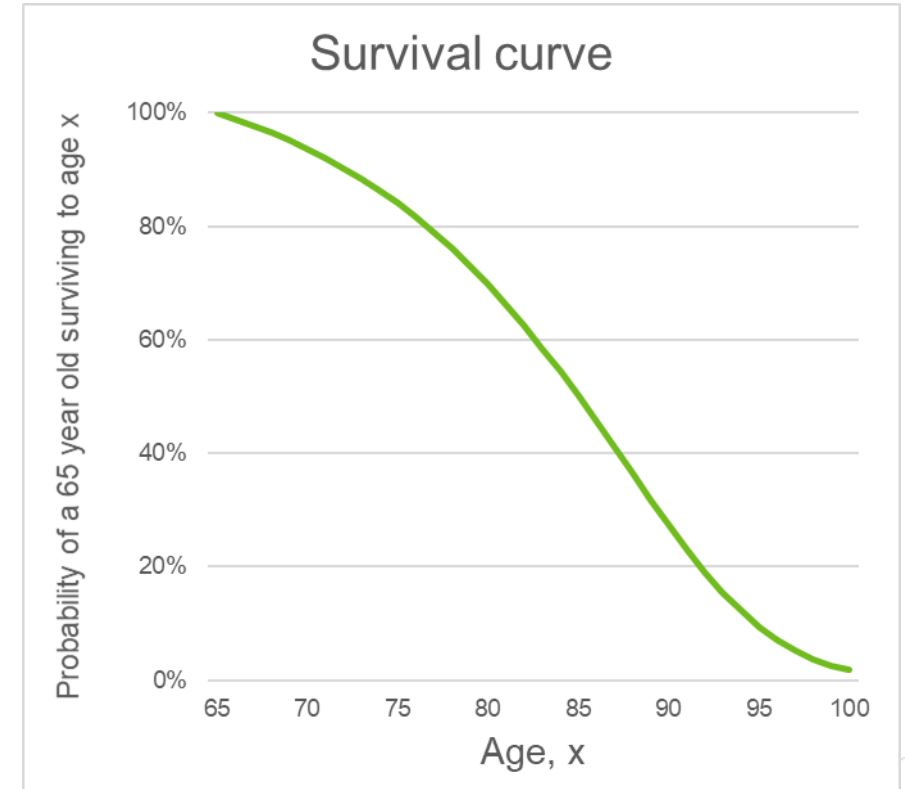
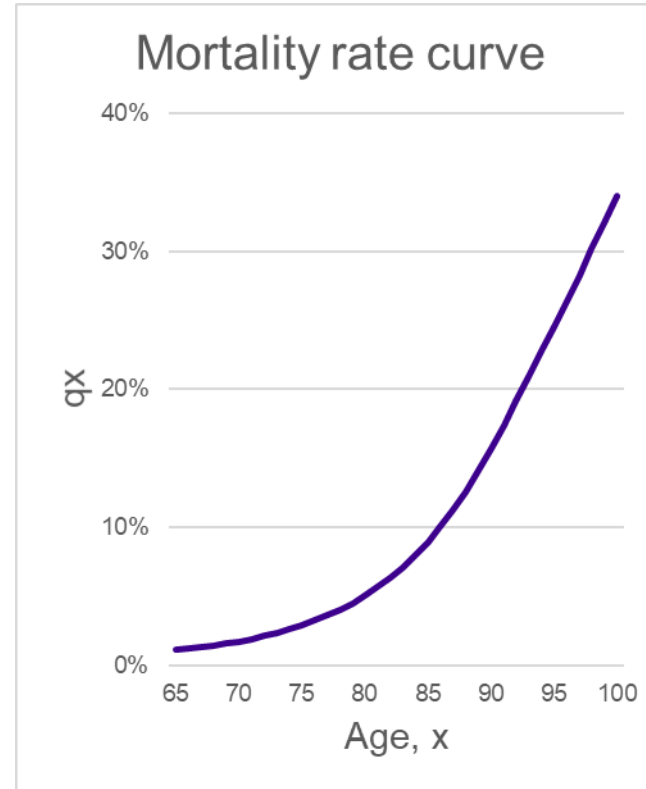
## Future trends

- How longevity will change in the future
- More subjective measure
- Recent experience a good starting point, but how and when will it change?



# What does a baseline assumption look like

Age ( $x$ )	$q_x$
...	...
57	0.724%
58	0.767%
59	0.808%
60	0.845%
...	...
89	14.079%
90	15.694%
91	17.391%
...	...
120	100%





# Different approaches

***“Top Down”  
approach***

**Collect large amounts of data  
from similar pension plans**

**Average out  
experience and  
apply to your  
plan**

**Your assumption**

***“Bottom Up”  
approach***

**Combine  
assumptions for  
the individuals  
within your plan**

**Calculate longevity for different  
individuals based on their characteristics**



## 2 Standard tables

# What are standard tables?

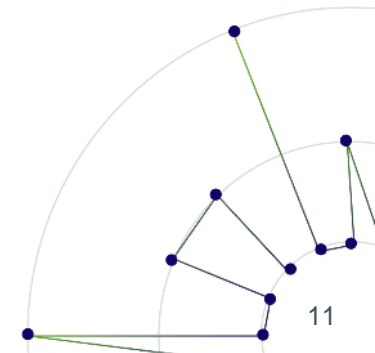


- Mortality base tables published by national agencies or actuarial bodies
- Constructed using a large portfolio, based on the expectation that they will be widely used across the industry.
- Separate tables are published for common risk classes
- "Top down" approach

Collect large amounts of data from similar pension plans

Average out experience and apply to your plan

**Your assumption**



# Using standard tables

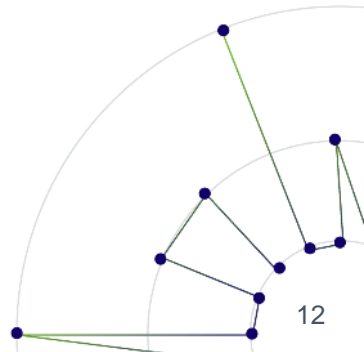
## When they are useful

- Plan-specific characteristics are “similar” to composite data in standard tables
- Small plan/limited experience - not sufficiently credible

## Limitations

- May not accurately reflect plan-specific characteristics
- Limited risk factors available for investigation
- Assessing sub-populations for risk transfer purposes

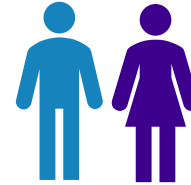
Reference population is rarely exactly appropriate to an individual plan's needs, so standard tables are often adjusted by applying an age rating or scaling factor.



# Data collection and segmentation



**Age**



**Gender**



**Collar Type**

Blue/White



**Sector Type**

Public/Private



**Pensioner Type**

Pensioner/Survivor



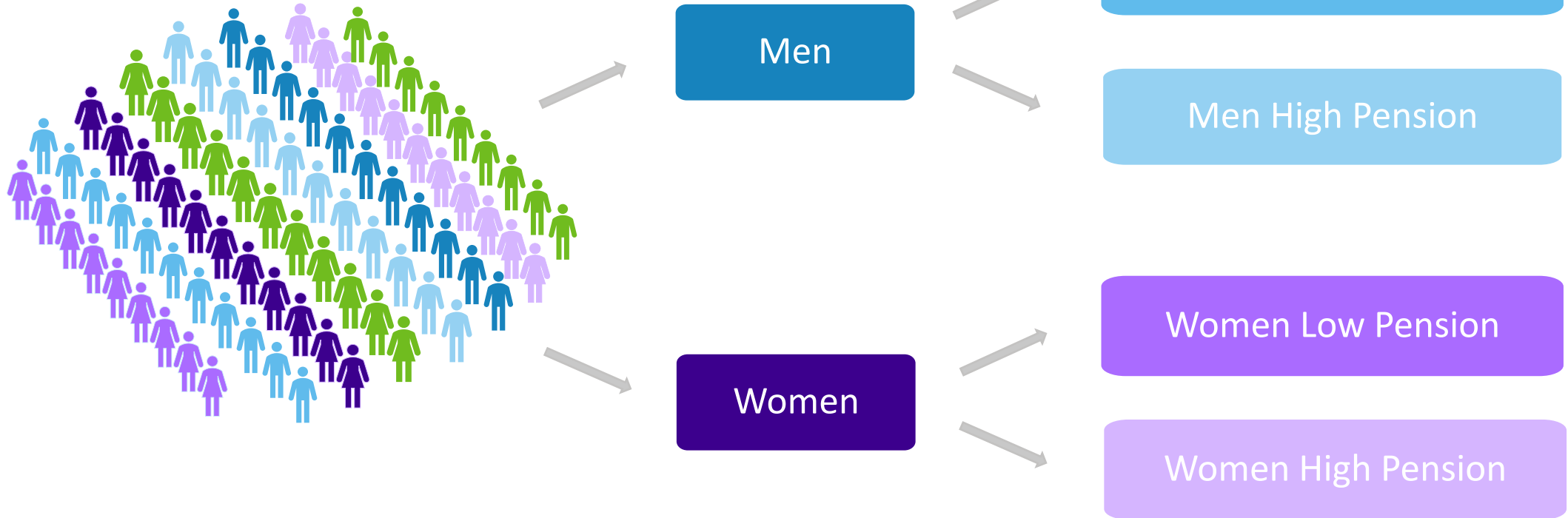
**Retirement-Health**

Normal/III-Health



**Pension Amount**

# Data collection and segmentation



Experience data is collected from a variety of pension plans, actuarial consulting firms and/or annuity providers

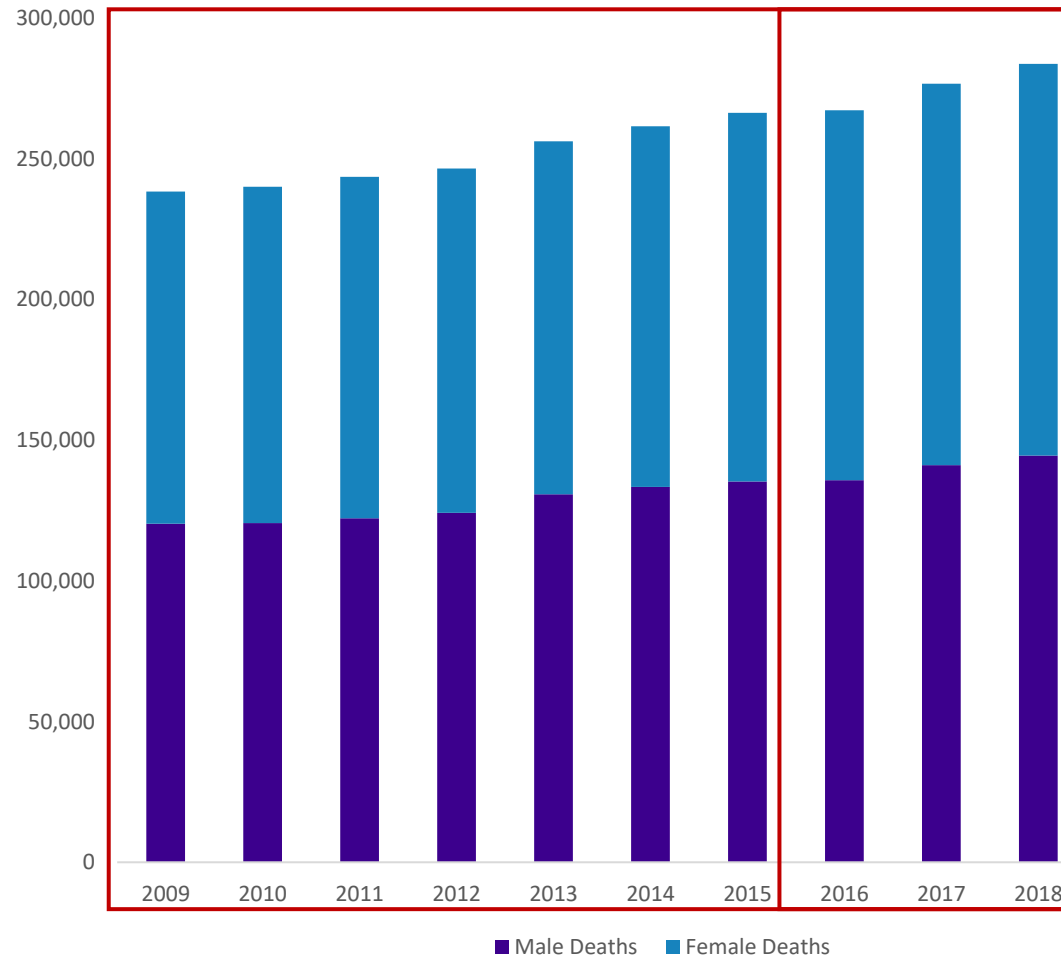
Data is summarized and *segmented* into risk factors with a standard table being produced for each subgroup



# Selecting the study period

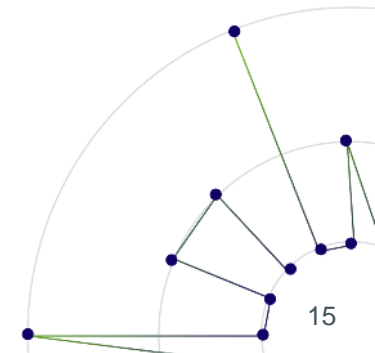
## Longer period

- Increases data volume
- Smooths out year over year volatility



## Shorter period

- More appropriate picture of current rates of mortality
- Better separation between baseline mortality rates and trend





# Calculating $q_x$ s

$q_x$

The mortality rate for age  $x$  - calculated as the number of deaths for exact age  $x$  divided by exposure for exact age  $x$ .

**Deaths**

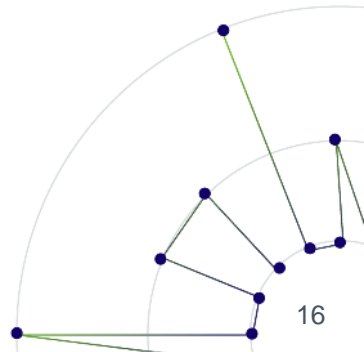
Number of people who died receiving a pension

**Exposure**

Measures the number of people receiving a pension who are “at risk” of dying

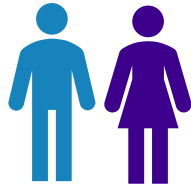
$$\frac{\text{Deaths}}{\text{Exposure}}$$

Crude/Observed  
Mortality Rate



# Lives-weighted vs amounts-weighted $q_x$

Lives-weighted or Headcount  $q_x$



$$= \frac{\text{Total Deaths}}{\text{Total Lives Exposed to Risk}}$$

Equal weight for each life

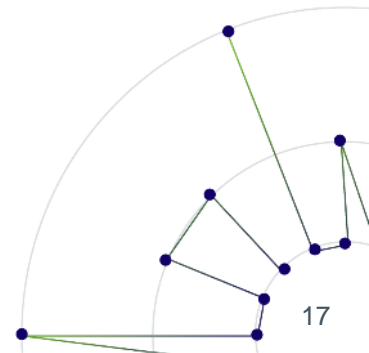
Amounts-weighted  $q_x$



$$= \frac{\text{Total Pension Amounts for Deceased Lives}}{\text{Total Pension Amounts for Exposed Lives}}$$

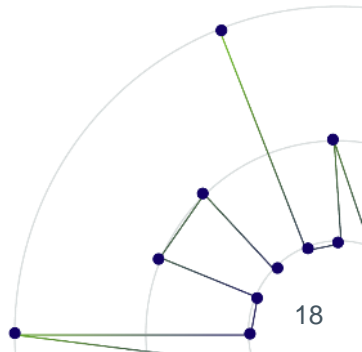
Weighted by pension amount

Amounts-weighted  $q_x$ s are lighter than lives-weighted  $q_x$ s hence they are more appropriate for valuing pension plan liabilities.



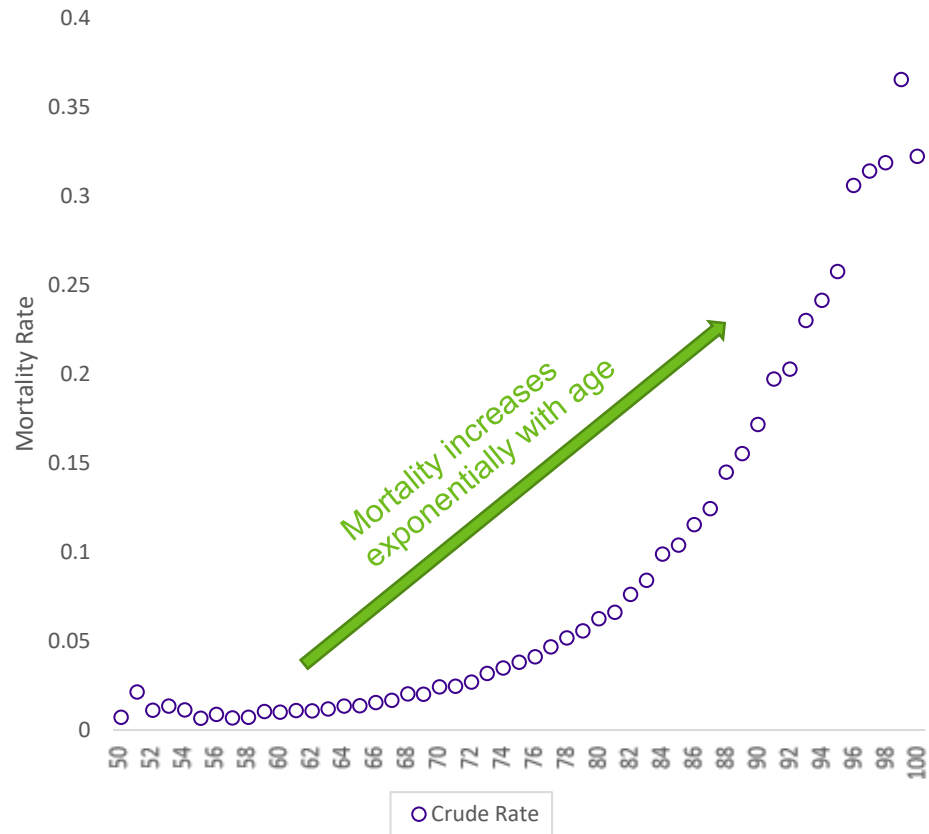
# Graduating tables

**Graduation** is the mathematical process of ironing out bumps in observed mortality rates at individual ages to produce rates that progress smoothly between ages.



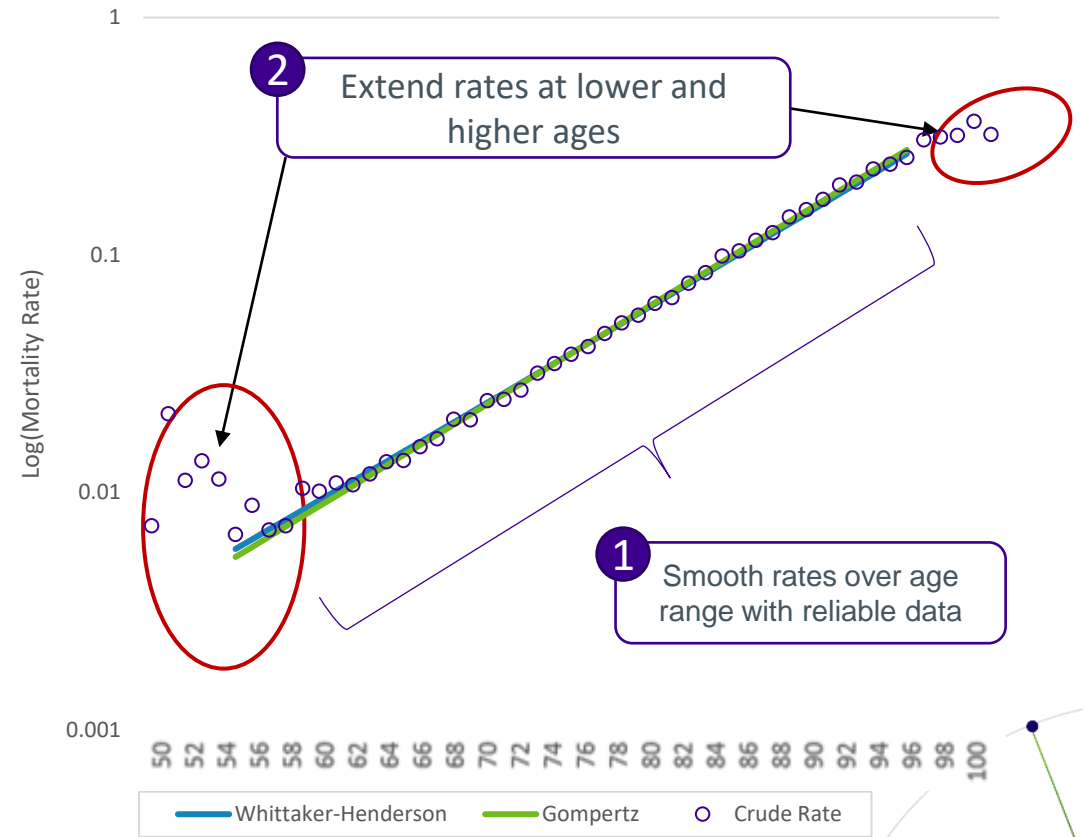
# Graduating tables

Crude Mortality Rates (Lives-Weighted) for CPM Males Private Sector






Transform to log scale so that rates are broadly linear with age

Illustration of Graduation of CPM Male Private sector (Lives-weighted), Logarithmic Scale



# Examples of different standard tables

				
Published by	Continuous Mortality Investigation (CMI)	Canadian Institute of Actuaries (CIA)	Society of Actuaries (SOA)	
Table Name	"S3" Series	CPM2014	Pri-2012	Pub-2010
Underlying population	Self-administered pension schemes (SAPS)	Canadian registered pension plans	US private-sector retirement plans	US public-sector retirement plans
Risk Factors	Gender Pensioner Type Retirement Type Pension Bands	Gender Sector Type <i>Pension Size Adjustment Factors</i>	Gender Pensioner Type Collar Type Top/Bottom Benefit Quartile	Gender Pensioner Type Retirement Type Employment Type Above/Below Median Income
Mortality Experience	2009-2016	1999-2008	2009-2014	2008-2013
Effective Date/Base Year	1 January 2013	1 January 2014	1 January 2012	1 July 2010

# 3 Factor based models

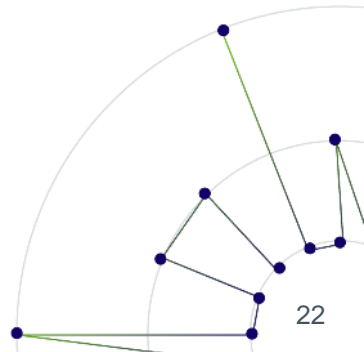
# Factor based models

- 'Bottom up' approach
- Consider factors which influence longevity
- Which should be modelled?
- Construct model to reflect those factors
- Allocate individuals based on their characteristics
- Overall assumption based on aggregating across individuals

**Your assumption**

Combine  
assumptions for  
the individuals  
within your plan

**Calculate longevity for different individuals based on their characteristics**





# What affects how long people live?



*Age*



*Gender*



*Affluence*



*Lifestyle*



*Health*



*Occupation*



*Location*



*Smoker?*



*Married?*



*Genetics*



# Data collection



*Age*



*Gender*



*Pension /  
salary*



*Postcode /  
ZIP code*



*Disability /  
ill health?*



*Manual /  
Non-manual*



*Location*



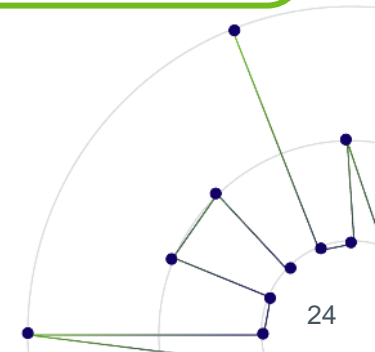
*Smoker?*



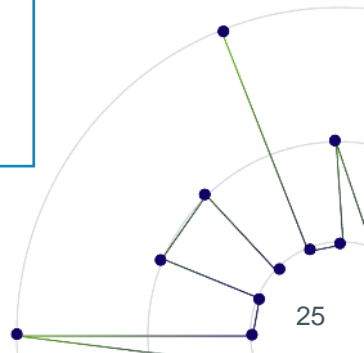
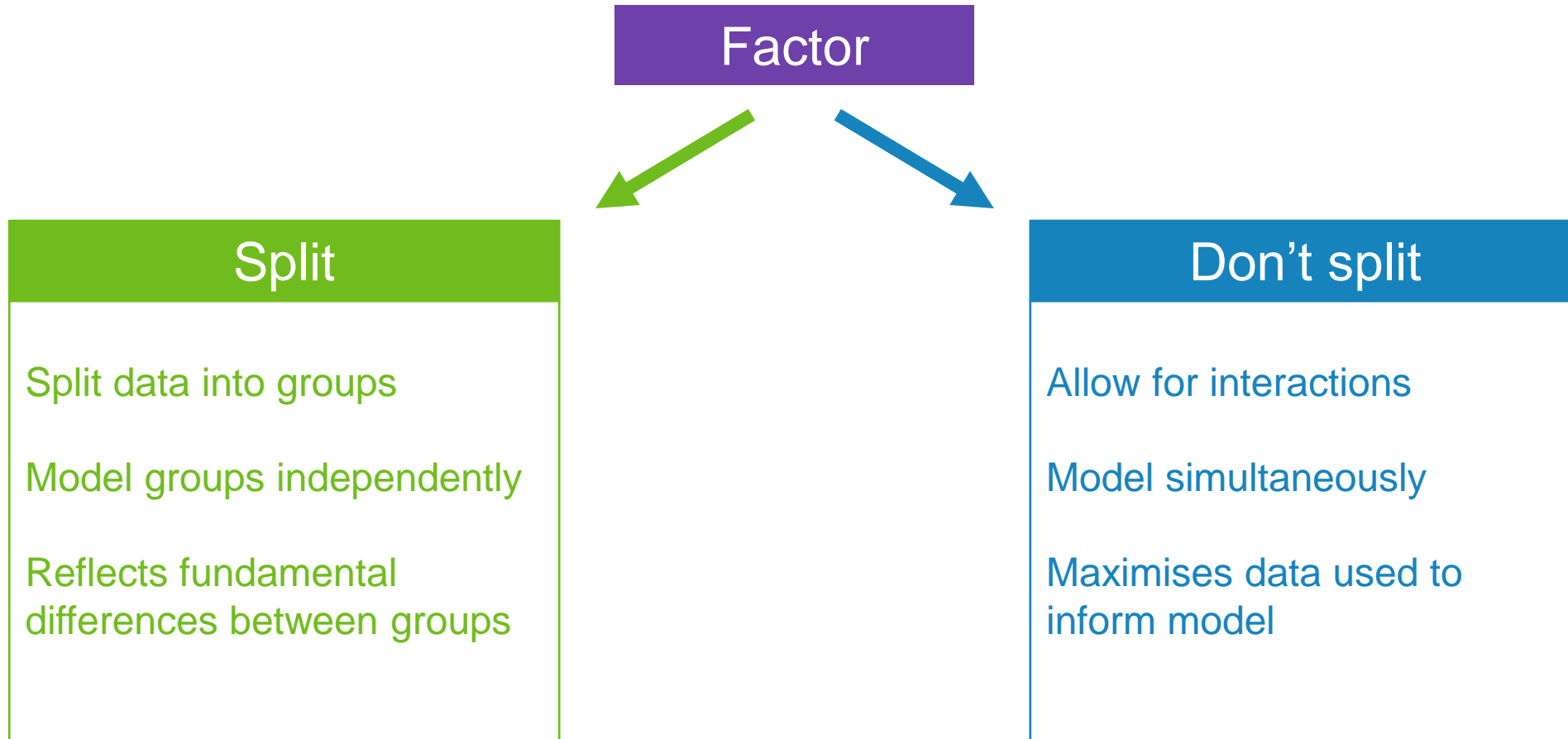
*Pension  
form*



*Genetics*



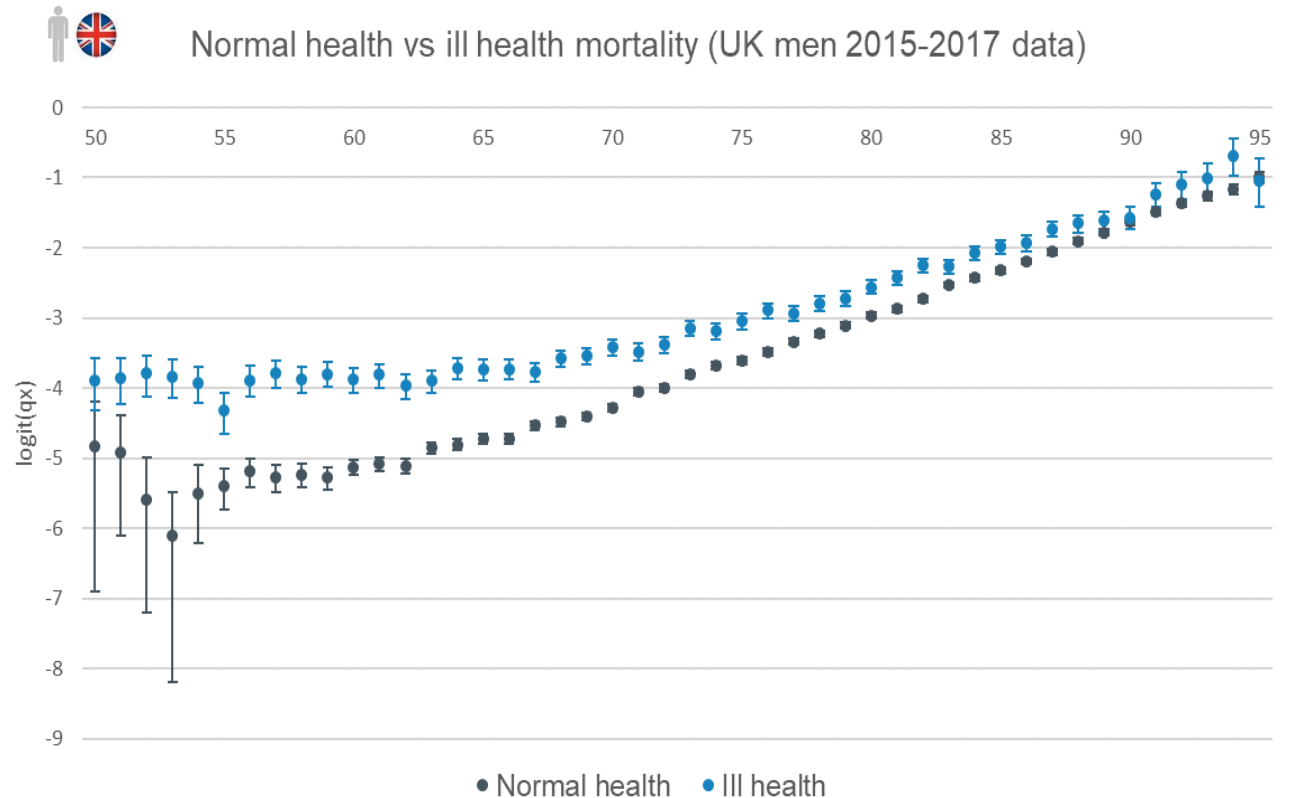
# Should we split the data?



# Splitting the data

Reasons to split the data (stratify):

- 1. Differences in shape**  
(e.g. normal versus ill health)
- 2. Difference in meaning**  
(e.g. pension amount for pensioners versus dependants)
- 3. Different age ranges**  
(e.g. dependants older than pensioners)



Source: Crude mortality rates with 95% confidence intervals, 2015-2017 Club Vita (UK) data

# Assigning variables

**Which** factors to use?

- How much 'extra' does each additional factor add?
- Does it justify extra complexity?

How to **assign** variables?

- **Number** of 'buckets' to use
- **Thresholds** for each bucket

Simplicity

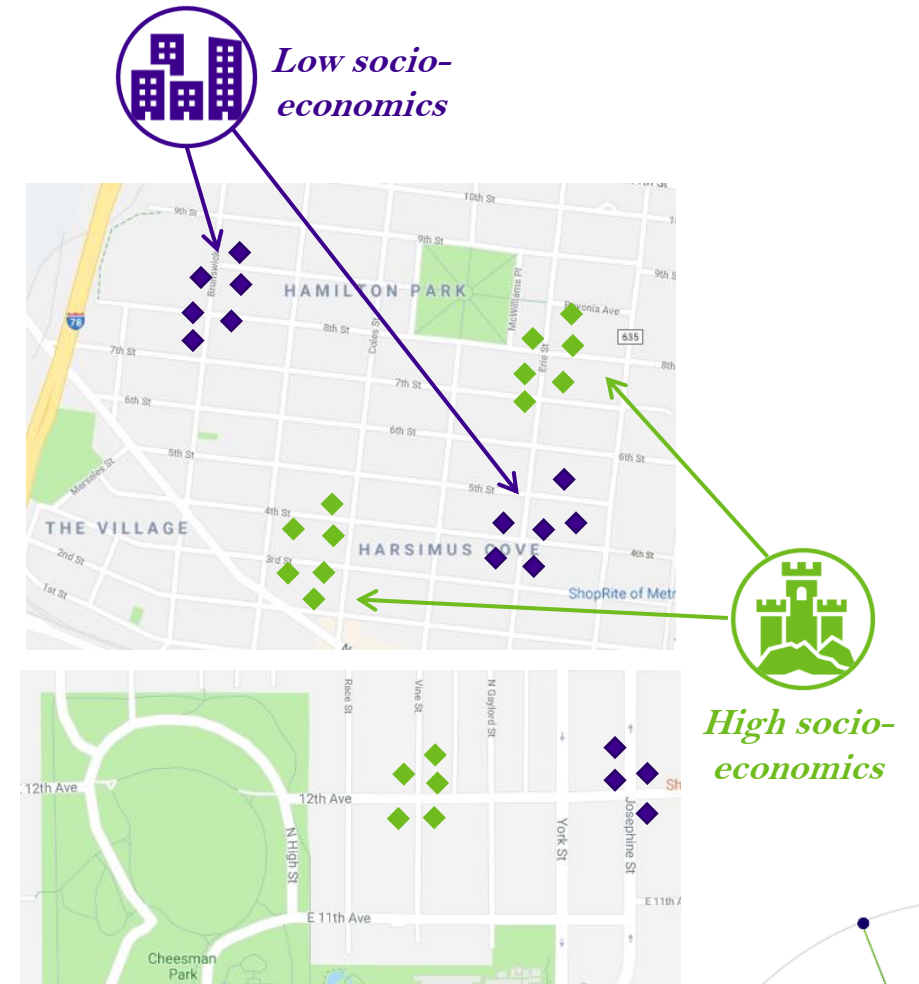


Predictiveness



# Grouping ZIP/postcodes

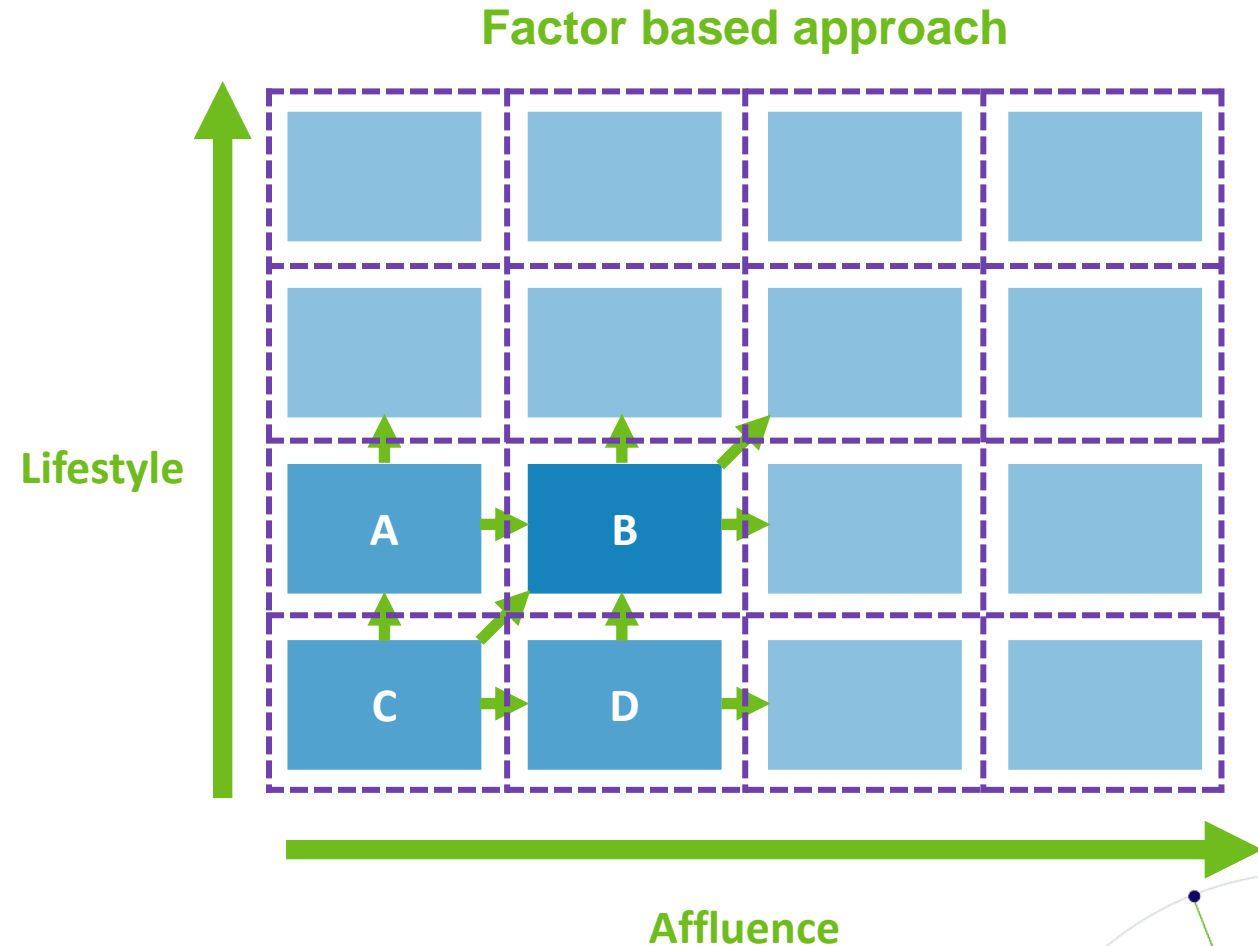
- Postal code is a proxy for lifestyle etc
- Residents in similar areas have similar characteristics
- Areas can be categorised by typical residents
- Similar areas exist in different parts of a country
- People with similar characteristics have similar longevity
- Postal code can be assigned to small number of groupings
- See our 'Zooming in on ZIP codes' paper for more details



\*Neighbourhood characteristics for illustration only

# Fitting the model

- Consider interaction of two factors
- Standard table approach:
  - each combination treated separately
  - very small ‘buckets’
- Factors based models:
  - allows for interactions between factors
  - maximises data used to inform fit

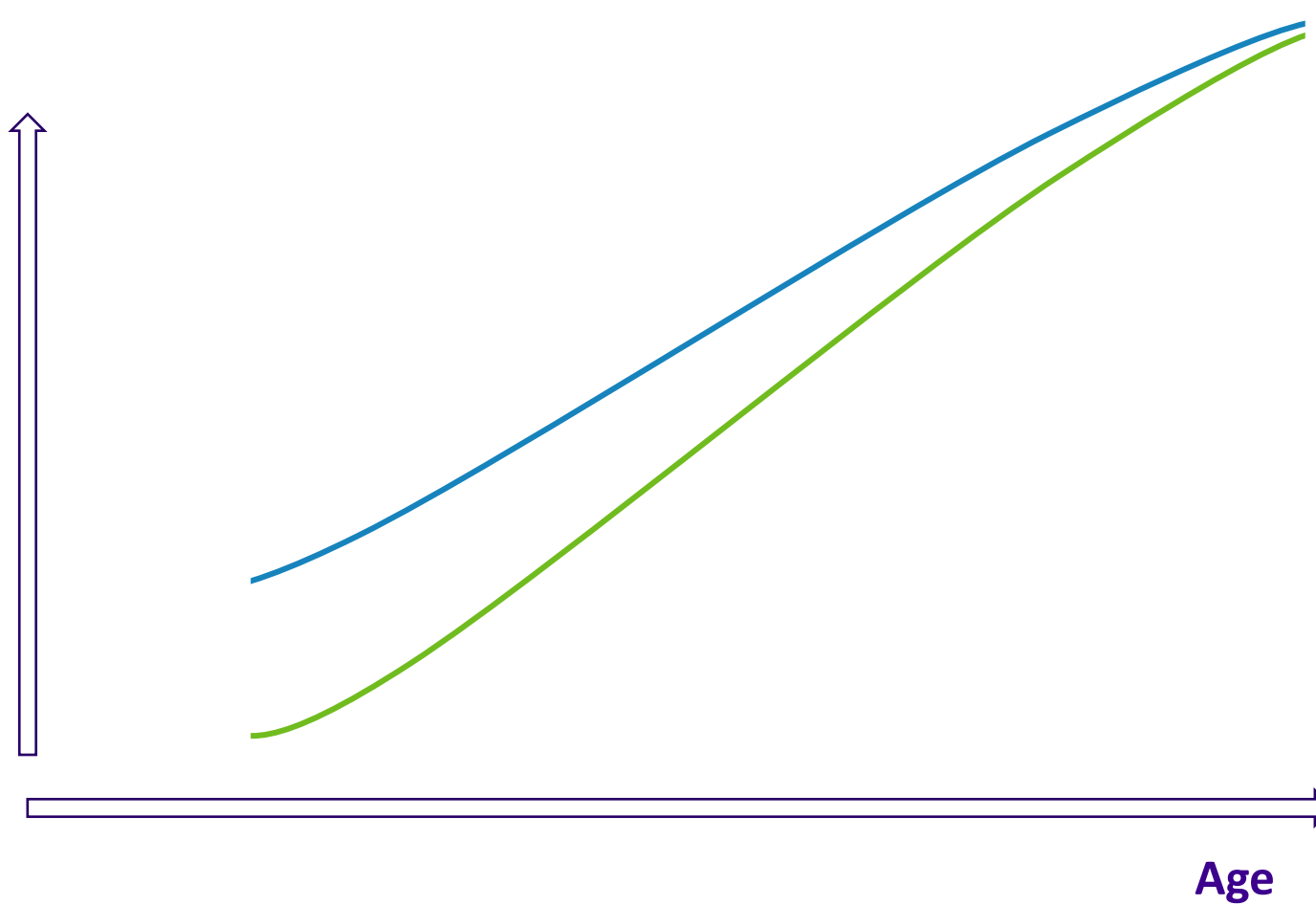




# Fitting the model

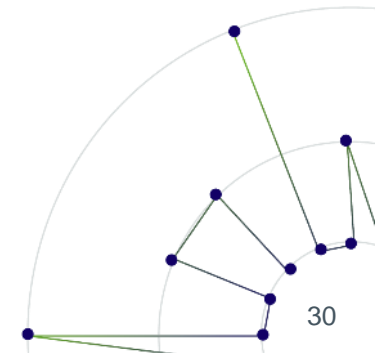
**Chance of dying over next year**

*Transformed onto a "log" or "logistic" scale so broadly linear with age*



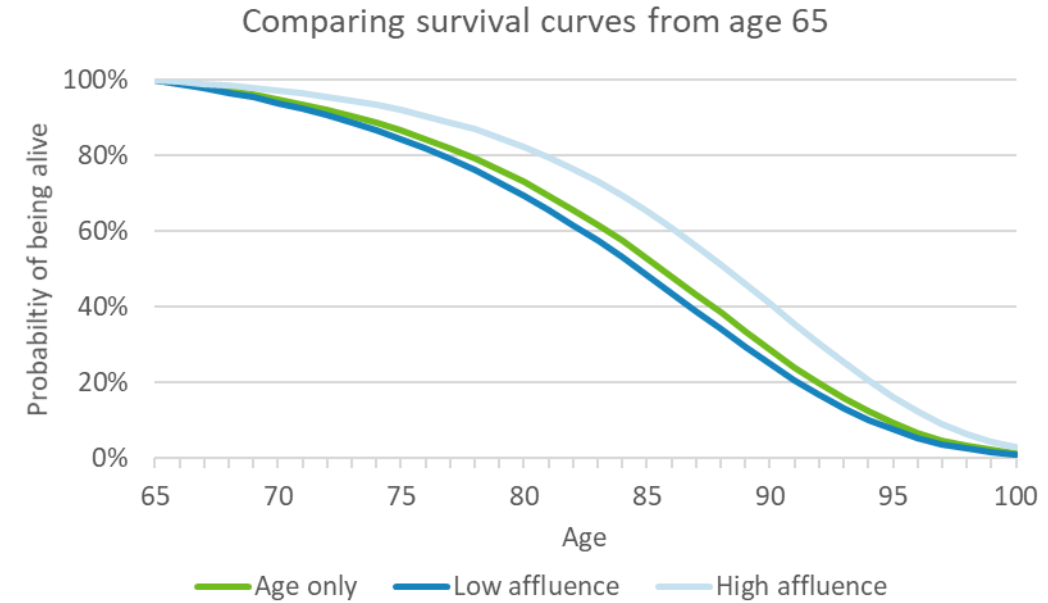
*Fit curves to across different combinations of affluence, postal code, occupation etc... simultaneously*

**Maximises the predictive power of the data**



# Checking fitted rates

- Important to validate generated rates
- Consider 'goodness of fit' to underlying data
  - Range of statistical, actuarial and validation tests applied
- Check internal consistency
  - Expect to increase with age
  - Curves in 'right' order
  - Less granular curves within extremes of more granular curves



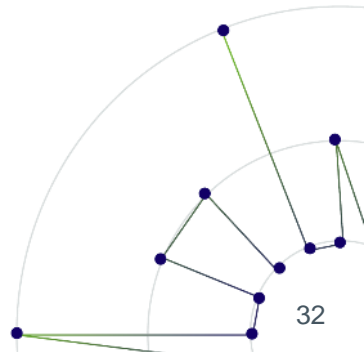
# Using factor based models

## When they are useful

- Reflect diversified nature of pension plan
- Better fit at individual level than 'average'
- Allow for changing demographics over time
- Smaller plans can benefit for wider 'pool' of experience data

## Limitations

- Dependent on data held by administrators
- Plan/Industry specific characteristics may not be fully reflected



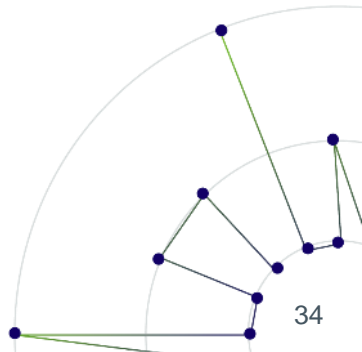
# 4 Experience analysis & credibility theory

# Overview

**What:** Comparison of *actual* deaths within plan to that *expected* under an assumption.

**When used:** To *confirm* appropriateness of proposed assumption.  
To *adjust* proposed assumption for known plan effect.

**Limitations:** *Generational stability* assumption.  
Seeking the perfect answer / *false confidence*.



# Explaining the jargon



A

**Actual** deaths experienced over the time period



E

**Expected** deaths experienced over the time period

A  
/\  
E

“A over E ratio”

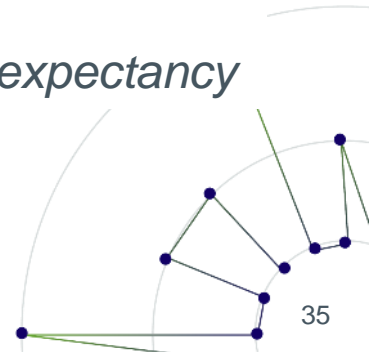
100%



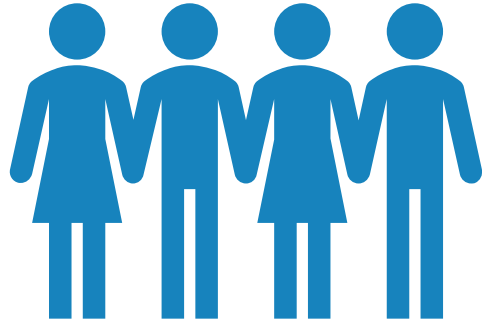
More deaths than expected  
Assumption **overstates** life expectancy



Fewer deaths than expected  
Assumption **understates** life expectancy



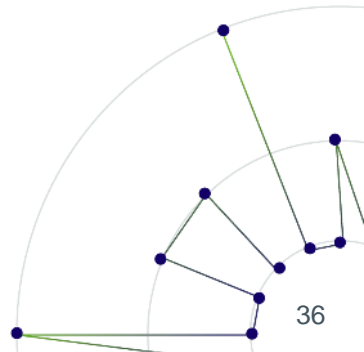
# “Lives” or “amounts”



**Lives**  
Number of people dying

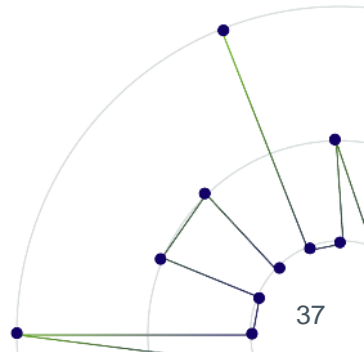
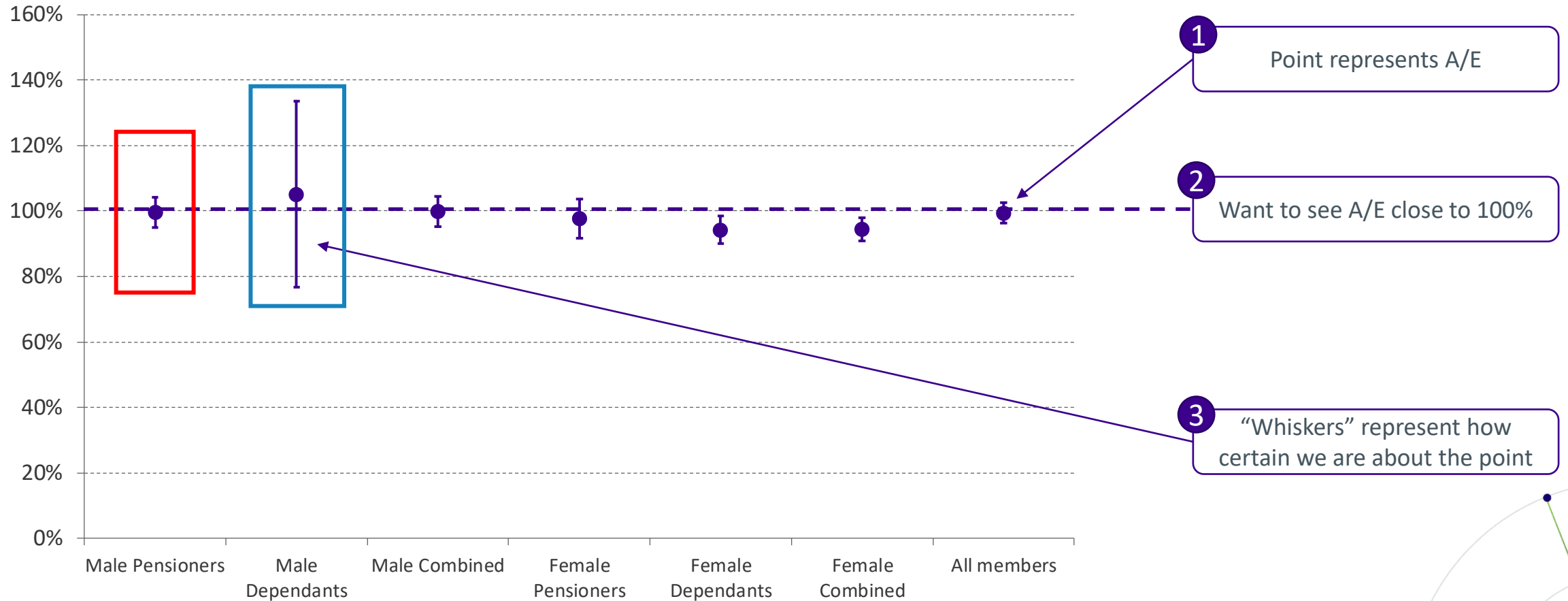


**Amounts**  
Amount of pension ceasing



# The “A over E” chart

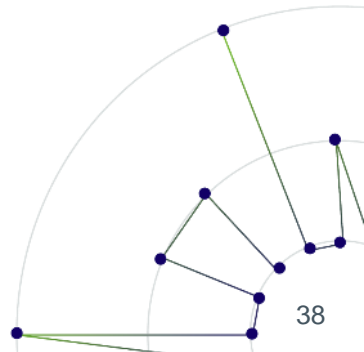
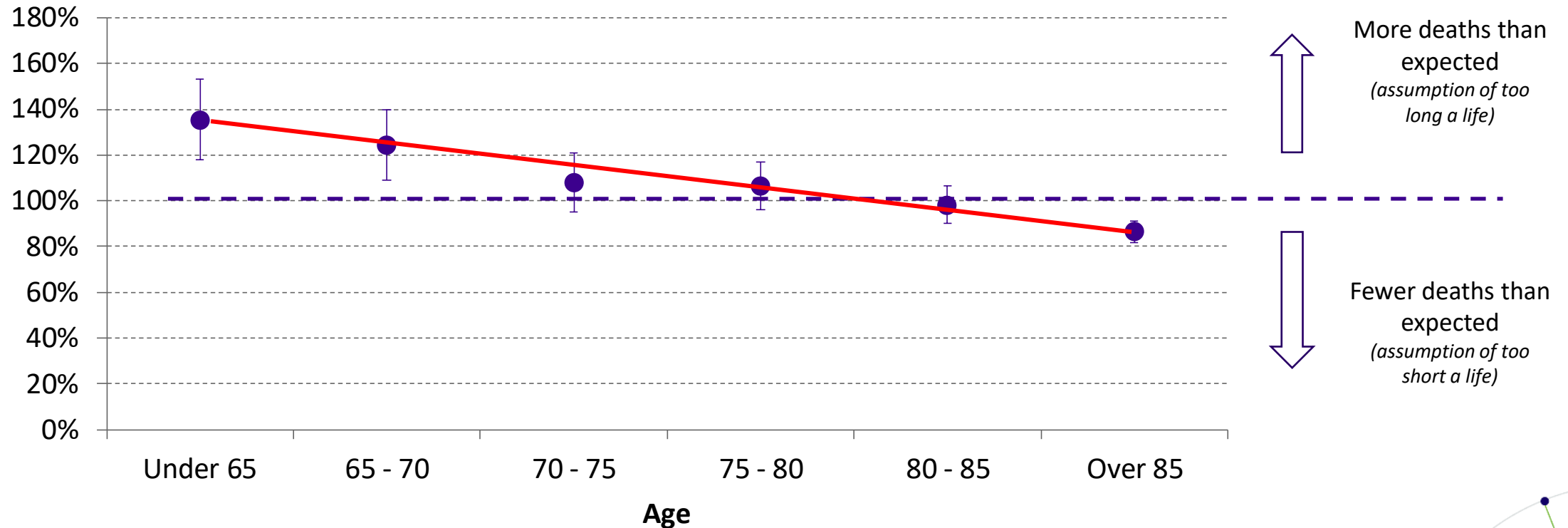
Overall amounts based A/E  
*Plan XYZ vs VitaCurves factor based model*





# Getting the age shape right

Actual compared to expected deaths on an amounts basis



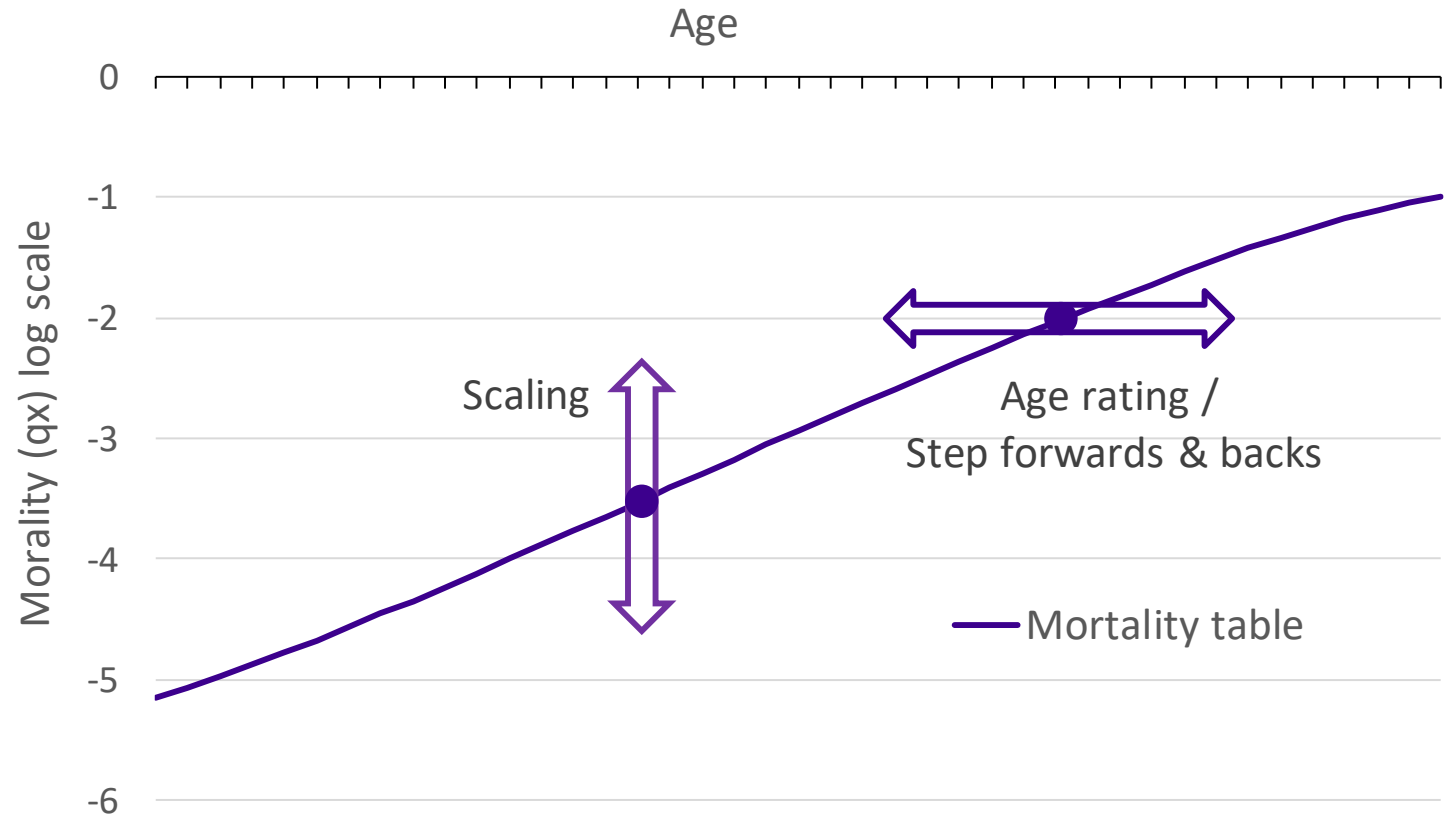
# Adjusting baseline to get A/E close to 1

## Scaling

120% \* rates in table

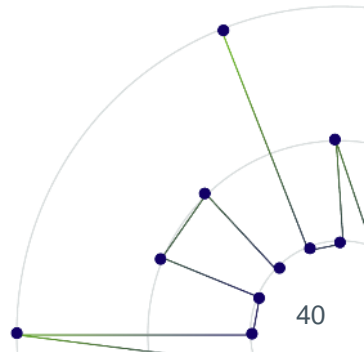
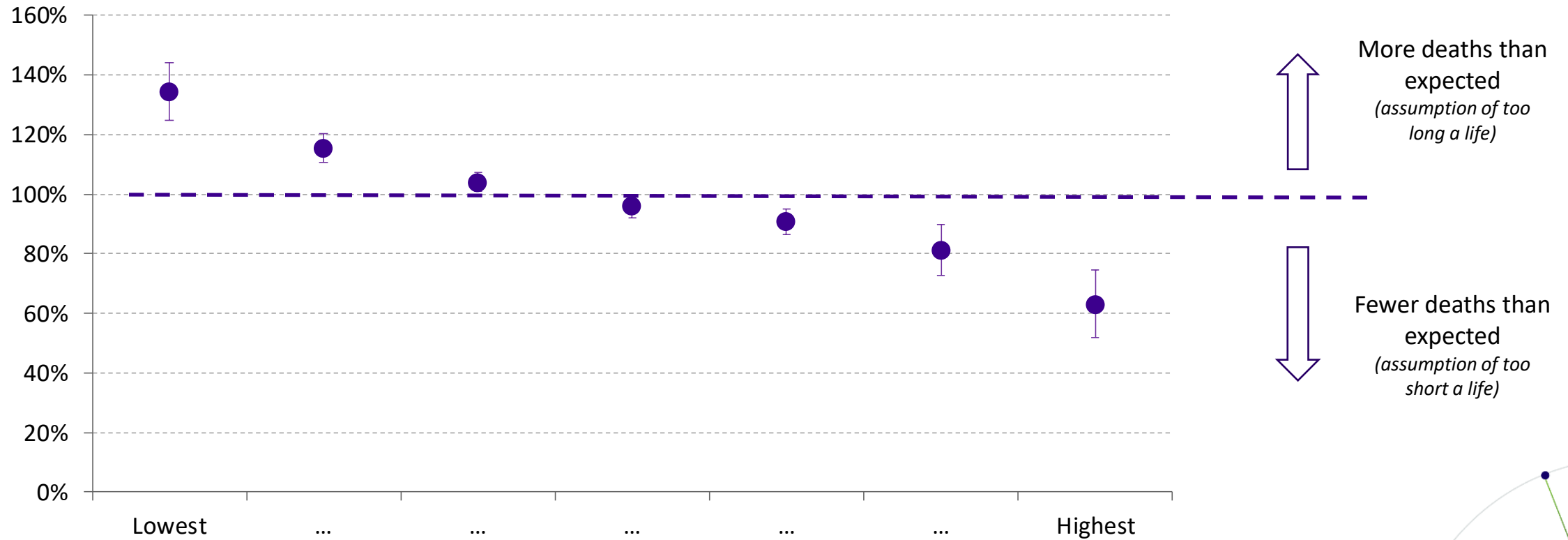
## Age rating / Step

Treat everyone is if  
3 years older

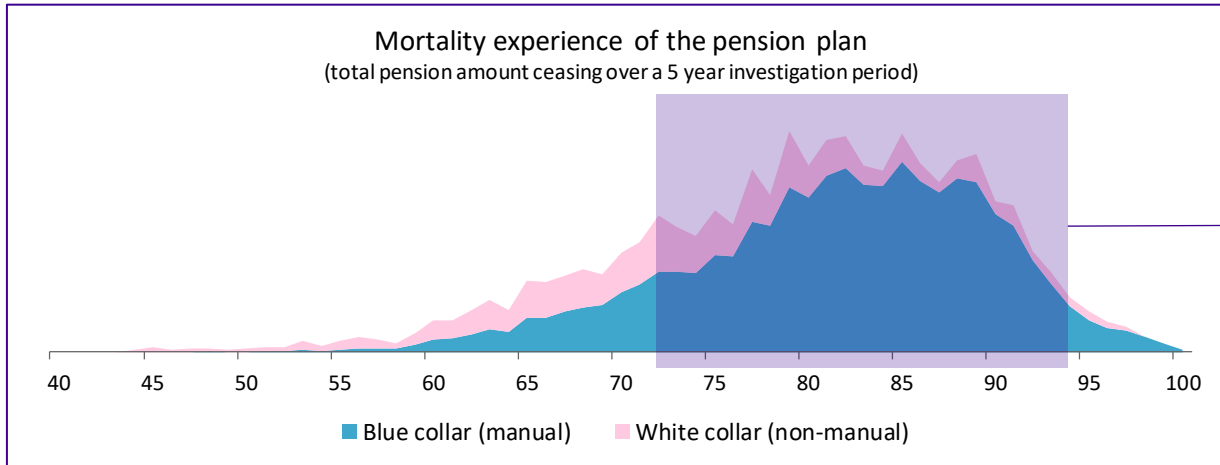


# Capturing diversity

Actual compared to expected deaths on an amounts basis  
(by benefit amount band)

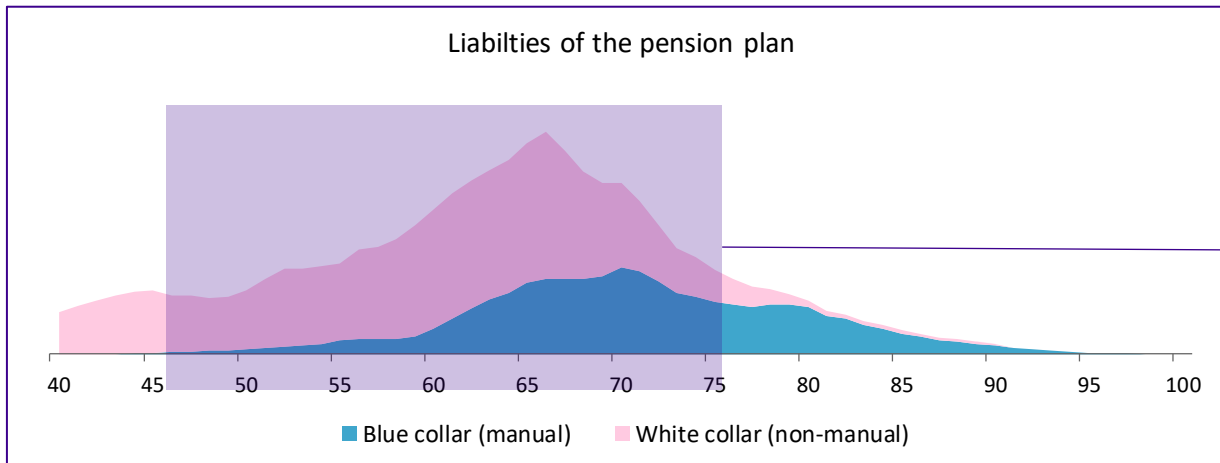


# Limitation: “Generational stability”



Experience analyses focus on where **most pensioner deaths occur.**

*For this plan this is a generation of **blue collar** workers*



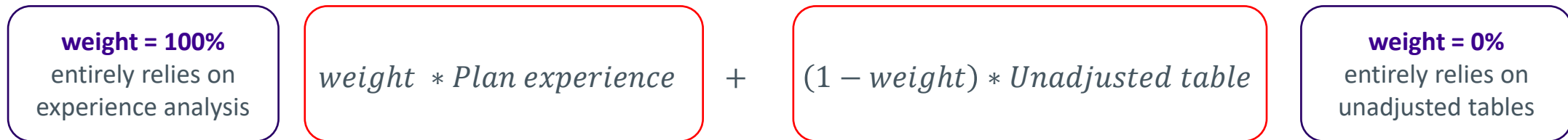
Many plans will have majority of liabilities relating to **younger lives**

*For this plan this is primarily **white collar** workers*

1. Ensure assumption underpinning experience analyses is able to pick up these differences
2. Smaller adjustments preferable (more likely to apply across generations)

# Applying credibility theory

- Mechanism for deciding how much **belief** to have in plan experience:



- Value of **weight** determined by a formula reflecting statistical confidence in unadjusted tables or experience analysis
- **Never** exactly 100% (“entirely self-credible”)
- **Guide only:** Lots of considerations including can you rationalise, data weaknesses etc...

Session 201 will explore issues in more detail



# Thank you

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